Conference Proceedings in Mathematics Education

Band 4

ALAN ROGERSON AND JANINA MORSKA (EDITORS)

THE MATHEMATICS EDUCATION FOR THE FUTURE PROJECT

PROCEEDINGS OF THE 15[™] INTERNATIONAL CONFERENCE THEORY AND PRACTICE: AN INTERFACE OR A GREAT DIVIDE?

4-9 Aug, 2019, Maynooth University, Kildare, Ireland

Bibliografische Information der Deutschen Bibliothek

Die Deutsche Bibliothek verzeichnet diese Publikation in der Deutschen Nationalbibliografießerflagatiliertissenformationen externationen über http://dnb.ddb.derabsufpar

Druck durch: winterwork 04451 Borsdorf http://www.winterwork.de/

Alle Rechte vorbehalten. Kein Teil des Werkes darf ohne schriftliche Einwilligung des Verlags in irgendeiner Form reproduziert oder unter Verwendung elektronischer Systeme verarbeitet, vervielfältigt oder verbreitet werden.

All Rights Reserved. No part of this publication may be reproduced, stored in a retrieval system, or transmitted in any form, electronic, mechanical, recording, photocopying, or otherwise, without the permission of the copyright holder.

Major Sponsors





https://www.meetinireland.com/

The Mathematics Education for the Future Project also wishes to thank for their support:

Budapest Semesters in Mathematics Education, the Education University of Hong Kong, DQME II, DQME3, MAV, AWM, AAMT, MACAS, MUED, Wholemovement, Mathematics Education Centre, Faculty of Sciences, Eötvös Lóránd University, Budapest and WTM-Verlag (Wissenschaftliche Texte und Medien – scientific texts and media).

Conference Organising Committee

Dr. Alan Rogerson, Poland/UK & Mgr. Janina Morska, Poland.

Local Organising Committee

Dr. Ciarán Mac an Bhaird (Chair), Dr Fiona Faulkner (Co-chair), Dr Mark Prendergast (Co-chair), Dr. Niamh O'Meara.

International Program Committee

Coordinator Dr. Alan Rogerson (UK/Poland). Prof. Miriam Amit, Ben-Gurion University of the Negev (Israel). Prof. Roberto Baldino, UNESP (Brazil). Dr. Andy Begg, Auckland University of Technology (New Zealand). Dr. Donna F. Berlin, The Ohio State University (USA). Prof. Ubiratan D'Ambrosio, Campinas/UNICAMP (Brazil). Prof. Bruno D'Amore, University of Bologna (Italy). Prof. Dr. Tilak de Alwis, Southeastern Louisiana University (USA). Prof. Paul Ernest, University of Exeter (UK). Dr Hanan Innabi, World Bank Consultant (Jordan). Prof. Nicolina Malara, University of Modena (Italy). Dr Maria Flavia Mammana, University of Catania (Italy). Prof. Dr. Ivan Mezník, Brno University of Technology (Czech Republic). Prof. Fayez Mourad Mina, Faculty of Education-Ain Shams University (Egypt). Prof. Catherine Paolucci, University of Florida (USA) Prof. Angela Pesci, University of Pavia (Italy). Prof. Dr. David Pugalee, University of North Carolina at Charlotte (USA). Dr. Arthur L. White, The Ohio State University (USA). Noor Azlan Ahmad Zanzali, IKRAM – Musleh, formerly of UTM (Malaysia). Wacek Zawadowski, Siedlce University (Poland).

Mathematics Education for the Future Project National Representatives

Prof. Gail Burrill USA, Prof. Maria Flavia Mammana Italy, Prof. Dr. Ivan Meznik Czech Republic, Dr. Hanan Innabi Jordan, Prof. Wacek Zawadowski Poland, Prof. Miriam Amit Israel, Prof. Noor Azlan Ahmad Zanzali Malaysia, Prof. Dr. Gunter Graumann Germany, Dr. Marjorie Henningsen Lebanon, Prof. Dr. Franco Favilli Italy, Prof. Gunnar Gjone Norway, Prof. George Malaty Finland, Prof. Willy Mwakapenda South Africa, Dr. Maria Luisa Oliveras Spain, Lionel Pereira-Mendoza Canada, Dr. Fatimah Saleh Malaysia, Prof. Anthony Sofo Australia, Prof. Teresa Vergani Portugal, Prof. Derrick Young South Africa, Prof. Angel Balderas Mexico, Dr. René Berthelot France, Dr. Cinzia Bonotto Italy, Dr. Jean Michel Hanna Egypt, Dr. Reda Abu-Elwan Oman, Assistant Prof. Othman Alsawaie UAE, Prof. Indira Chacko India.

Our Project and Conference Webpages

- Our Project Home Page: <u>http://math.unipa.it/~grim/21project.htm</u> has the proceedings of previous conferences from Egypt 1999 to Dresden 2009.
- Andreas Filler at http://www.afiller.de/charlotte07 has a photo album of our Charlotte Conference in 2007.
- For recent conference links please email <u>alan@cdnalma.poznan.pl</u>

Foreword

This volume contains the papers presented at the International Conference: *Theory and Practice: An Interface or A Great Divide?* held from 4-9 August, 2019 at Maynooth University, Kildare, Ireland.

The Conference was organized by The Mathematics Education for the Future Project - an international educational project founded in 1986 and dedicated to the improvement of mathematics education through the publication and dissemination of innovative ideas. Many prominent mathematics educators have supported the project in the past including: Hans Freudenthal, Andrejs Dunkels, Hilary Shuard, Bruce Meserve, Marilyn Suydam, Alan Osborne, Margaret Kasten, Mogens Niss, Tibor Nemetz, Ubi D'Ambrosio, Brian Wilson, Tatsuro Miwa, Henry Pollack, Werner Blum, Roberto Baldino, Waclaw Zawadowski.

Deserving Scholars and Researchers Programme

For the fourth time in our conferences deserving scholars were invited to submit papers for peer review and publication in the proceedings even though they were unable to attend the conference itself. Instead, their papers were included in the conference programme and were briefly presented by others. The papers in Maynooth were those by: Dr. Maifer Remzie Demirbec, Bernie (Dov) May and Dr. Esther Pearson. Since we will not meet these authors face to face in Ireland we have included their photographs and short CVs at the end of these Proceedings and in the permanent Ireland Conference Documents webpage.

We sincerely thank all of the contributors to the conference for their time and creative effort. It is clear from the variety and quality of the papers that the conference has attracted many innovative mathematics educators from around the world.

We are especially grateful to Professor Martin Stein of Münster University, the Owner and Manager of the company that publishes these printed proceedings: WTM-Verlag (Wissenschaftliche Texte und Medien – scientific texts & media).

These Proceedings begin with the Plenary Paper and Workshops by Douglas Butler, followed by a contents list and then the papers & workshop summaries in alphabetical order of the principal authors.

Dr. Alan Rogerson D.Phil (Oxon), M.Sc., B.Sc., B.A. (Lon), Dip.Ed., Cert. Ed. (Cantab). Chairman of the IPC and Co-ordinator of the Mathematics Education for the Future Project

Plenary Keynote Address: Can Technology make a Difference to Mathematics Education?

Douglas Butler iCT Training Centre, Oundle UK <u>debutler@argonet.co.uk</u>

Douglas has followed the introduction of technology in the mathematics classroom from the start in the 80s to where we are today. There is now a massive spectrum of wonderfully sophisticated tools to help make mathematics lessons shine for today's inter-connected students. The possibilities are endless, and with A.I. just around the corner ... yet the majority of mathematics teachers are not using digital resources at all. This session, and the two workshops to follow, will attempt to answer this by referring to research in this area, and by showing some spectacular lesson plans in which the technology does not get in the way, and the mathematics shines through.

Workshop 1: Helping Statistical Education through Visualisation

Statistics is rapidly being adopted as a major section of school syllabuses. This workshop will start by showing where to find thought-provoking large data sets. Douglas will then show how the latest incarnation of Autograph makes light work of the analysis and helps students to make sense of what's going on by the use of dynamic visualisations.

Workshop 2. Exploring Concepts through a Friendly User-interface.

There are now three major players in graphing technology for mathematics education. They are, in order of seniority: Autograph, Geogebra and Desmos. Each has their strengths. This workshop aims to illustrate how the userinterface of the latest incarnation of Autograph has been designed particularly with the pedagogical process of teaching and learning at the forefront.

Douglas Butler has enjoyed a full life in mathematics education, as a teacher, head of department, chairman of MEI, organiser of TSM Workshops for over 25 years, and he has spearheaded the continued development of the ever

popular software Autograph. When not doing any of this he enjoys sailing his Wayfarer, and conducting the Rusty Strings of Oundle!

Table of Contents		
	v	
Plenary Keynote Address by Douglas Butler Can Technology make a Difference to Mathematics Education?	.vi	
Fouze Abu Oouder & Miriam Amit		
Incorporating Ethnomathematical Research in Classroom Practice-		
Nadine Adams & Clinton Hayes Providing Synchronous Mathematics Instruction to Distance		
Students- Workshop		
Kehinde Emmanuel Adenegan		
Cynthia O. Anhalt & Ricardo Cortez Mathematical Modeling Thinking: Laving the Foundation for Mathematical Modeling		
Competency		
Glenda Jean Ashleigh		
Individual Differences in Cognition and Affect in Multiplicative		
Katarzyna Banach Ok Notebook as an Untypical Form of Student's		
Notebook - Own Experience		
Summer Bateiha & Sadia Mir		
Engaging with Mathematics through Three Types of Storytelling29		
Mike Bedwell Freedom of Speech 34		
College Students' Views of Fraction Arithmetic		
Paul Betts et al		
Foundational Experiences as a Design Principle for Mathematics Curriculum for		
Gilidieit		
Esther Billings & Lisa Kasmer Learning via Teaching: Examples of Mediated Field Experiences		
in Early Coursework of Pre-service Teachers		
Daniel J. Brahier		
Research into Practice: 29 Years of Classroom Teaching54		
Sandra Browning Elementary Preservice Teachers and Questioning Strategies in		
Mathematics		
Gail Burrill		
Statistical Literacy and Quantitative Reasoning66		
Advantages, Challenges and Opportunities in Teaching Statistics		
in Doctoral Training to a Heterogeneous Group: the Case of		
Luis Alexander Castro Miguez et al Diagrammatic Reasoning from Reflections on Peircean Semiotics78		
Olive Chanman & Paulino Preciado Babh		
Prospective Secondary Mathematics Teachers' Development of Knowledge of Modelling for		
reaching		
Kin Eng Chin & Fui Fong Jiew Misconceptions or Preconceptions in Making Sense of Decimals 90		
Supporting Mathematics Teachers to Build Deep Understandings		
of the Home Contexts of their Students96		

Katharin	e Clemmer et al Collaborative Solution Discovery: A Problem Solving Process100
Porter Co	oggins et al The Mathematical Culture of Ojibwe Students-An Ethnographic Study104
Ken Coll	ins Using CAS to Improve Student Understanding of Calculus Concepts110
Marjorie	Curry Culturally Responsive Math115
Bronisla [,]	<mark>w Czarnocha</mark> Constructivist Teaching Experiment: Constructivist Research and Constructivist Teaching118
Mili Das	Curriculum for Mathematics Education – An Approach to Discuss Relation Between Theory and Practice
<mark>Jan de L</mark>	ange Curious Minds: Serious Play130
Maifer R	<mark>emzie Demirbec</mark> Puerto Rico Gas Prices Fall – "The Math of Cheap Oil"136
Thomas	P. Dick & Mary E. Pilgrim Learning (and Learning Teaching) by Doing Problems139
Pam Dor	<mark>rington</mark> Family Maths: Experiential Learning
Daniela I	Ferrarello et al Serious Games in Teaching/learning Mathematics: the Experience of FunGo150
Benjamiı	<mark>n Fine et al</mark> The Impact of Mathematics and Mathematicians156
Courtney	<mark>/ Fox</mark> Clean Water for Women and Children161
Ben Gall	<mark>uzzo & Katie Kavanagh</mark> Getting Started Getting Students Modeling: Designing and Facilitating Open-ended Math Modeling Experiences164
Avikam (<mark>Gazit</mark> Math Teachers' Attitudes toward Integrating Humor in Math Lessons168
<mark>Eoin Gill</mark> Ma in I	ths Week Ireland: Promoting a Positive Attitude to Mathematics reland173
Joanne E	E. Goodell Learning to Teach Mathematics Through Project-Based Instruction177
John Go	<mark>rdon et al</mark> A Problem-Solving Approach to the Introduction to Ordinary Differential Equations for Undergraduate Students at an American Two-year College183
<mark>Ivona Gr</mark>	<mark>zegorczyk</mark> Magic Tricks and Activities Supporting Abstract Thinking in Mathematics189
Irina Gur	evich Do Future Mathematics Teachers Need the Course "Integration of Digital Technologies in Teaching Mathematics", and if so, what exactly can it help them with?193
Heidi B.	Hansen & Marta T. Magiera Working Together: A Cross-cultural Study Addressing Mathematics Anxiety in K-8 Pre-service Teachers

Bradford Hansen-Smith

Why the Circle cannot be Squared......205

Janet M.Herrelko

Change the Paradigm of Solitary Lesson Planning to Collaborative Planning that Unites Research and

Kenneth Horwitz

Utilizing Analytics to show Representations used in Comparing and Ordering Unit

Hsin-Mei E. Huang et al

Investigating Junior High School Students' Length Estimation Ability

Yuitza T. Humarán Martínez

Using Manipulatives to Develop the Understanding of the Concept of the Fraction of Preservice Elementary Teachers: The Meaning

Debra L. Hydorn

Tools for Modern Mathematics: A Course to Introduce Experimental

Clement O. Iji & Joseph A. Andortan

Brandishing Ethno-Mathematics Approach as an Interface for Improving Upper Basic Education (UBE) Students' Interest and Achievement in Number and Numeration.....240

Hanan Innabi et al

Patterns of Variation in the Work of "Mathematics in the City Project": A Suggested Research Question......245

Colin Jackson

Going Against the Grain: Critical Thinking in and Beyond

Fui Fong Jiew & Kin Eng Chin

The Embodiment of Mathematical Meanings with Special Reference

Peter Johnston et al

Supporting Transition for Mathematics and Science Students under

Sue Johnston-Wilder & Clare Lee

How can we Address Mathematics Anxiety more Effectively as a Community?

Luckson Muganyizi Kaino

Enhancing Mathematical Modeling Activities in Classroom

Sylwia Kania

Solving Mathematical Problems in the Context of Some Obstacles between Teachers and

Tierney Kennedy

Exploring the Nature of Teacher Questioning within Challenging

Sergiy Klymchuk & David Wilson

Integrating Pen-enabled Tablet PCs in Teaching Engineering

Steve Krevisky

Using Sports Data in Statistics and Math Classes: An Overview

Satoshi Kusaka

Analysis of the Characteristics of Mozambican Primary Mathematics Textbooks compared with Japanese Textbooks focusing on Tasks

275

Katie Laskasky et al

Innovative Problem Solving: What happens when Math Education, Business, and Engineering Perspectives

Collette Lemieux & Eric Roettger Students' Reasoning During a Calculus Two-Stage Exam

Olderna Reasoning During a Calculus Two-Olage Exam	
Olga León Corredor et al	
Integrating Technology and Didactic Resources for Enhancing	
Learning Processes. An Exploratory Study	318
Su Liang	
Enquiry-Based Learning in College Mathematics Education:	
Theory and Practice	324

Alenka Lipovec & Jasmina Ferme

Some Factors Influencing Effectiveness of Mathematics

Michael Lousis

Patricia Marchand

312

Urška Markun & Jasna Kos

Małgorzata Mart

Ralph Mason *et al*

Bernie (Dov) May

ngage Students More Hopscotch Math has Students Jumping for

Petra Menz & Nicola Mulberry

Claus Michelsen

Marguerite K. Miheso-O'Connor

Jenny Missen

13

Shelby Morge

Addressing Teachers' Culturally Responsive Teaching Beliefs	
through Course Activities	392
J. J	
Janina Morska	
From the Purpose of the Lesson to Success	398

Lio Moscardini *et al*

Collaborating Across the Pond: Cognitively Guided Instruction	
Project	401

Nitsa Movshovitz-Hadar *et al*

Bridging between School Mathematics and Contemporary Mathematics: Turning a Dream into Reality......407

Ajayagosh Narayanan

Peer Tutoring: Developing and Sustaining Effective Teaching	
Practices with Mathematics Teachers in Lesotho	

María Estela Navarro Robles

Variation Theory used to make a Personalized Diagnostic in the Level of Knowledge of Fundamental Concepts about Rational Numbers and their Operations in Undergraduate Students.......419

Margaret L. Niess

Online Strategies Enhancing Mathematics Teacher Knowledge for the Digital Age: Discourse and Critical Reflection423

Jenna R. O'Dell & Todd R. Frauenholtz

An Unsolved Graph Theory Problem: Comparing Solutions of

Grades 4, 6, & 8......429

Niamh O'Meara & Fiona Faulkner

Jenny Pagge

Catherine Paolucci

Supporting Pre-service Mathematics Teacher Development through Transformative Community Engagement.......446

Catherine Pearn *et al*

Developing and Assessing Algebraic Reasoning in the Middle Years..451

Esther Pearson

STEPS" to a Brighter

Mary E. Pilgrim & Thomas P. Dick

Actively Engaging in Calculus to Support all Students......463

Ildikó-Anna Pomuczné Nagy

Hilary Povey

Mark Prendergast et al

Shagufta Raja et al

Using GIS to Develop Spatial Reasoning and Analysis of Data.......486

John R. Ramsav

Mentored Teams of Undergraduates in Real World Consulting.........492

Marina Rugelj

Jacqueline Sack & Judith Quander

Adalira Sáenz-Ludlow & Alexandra Jiménez Jiménez

Linkages between a Teacher's Preparation and the Potential for Students'

Learning......510

S. R. Santhanam

Josephine Shamash

Dennis Showers

Atara Shriki & Ilana Lavy

Timothy Sibbald

The Confluence of Numeracy with Interdisciplinary Mathematics......530

Dianne Siemon

Connecting Research and Practice – The Case of Multiplicative
Thinking

Raymond Smith et al

Insights Gained from Implementing Teaching Toolkits: A Case of Activating Prior Knowledge......542

Kerri Spooner

Max Stephens

Tadashi Takahashi

Proving in Mathematics Education - On the Proof using ATP -559

David Tannor

Barbara Ann Temple et al

Jeffrey Thomas

José A. Toro-Clarke

Ariana-Stanca Văcăreţu

Thomas Walsh Jr

Thomas Walsh Jr.

Lynae Warren & Kay Wohlhuter

Steven Watson

Lyn Webb et al

Enabling Grade 3 Teachers to Transform an Intended Curriculum into an Enacted Curriculum in Mathematics Classrooms.......614

Paul Webb

Gregory A. Wickliff et al

lan Willson

Stephen Woodcock

Not all Equals are Equal: Decoupling Thinking Processes and

Simon Zell

Weekly 10-minute-tasks to Promote Students Solving Equations in a Content-oriented

Alan Zollman

Ryan G. Zonnefeld & Valorie L. Zonnefeld Innovative Pathways in STEM Teacher Preparation: Bridging the Gap between University Expectations & Secondary School Needs......650

Deserving Scholars & Researchers, Maynooth, 2019......653

Please Note: Papers in Blue Highlighting were not presened by the authors at the conference.